

CHAPTER 10

THERMODYNAMICS

WORK

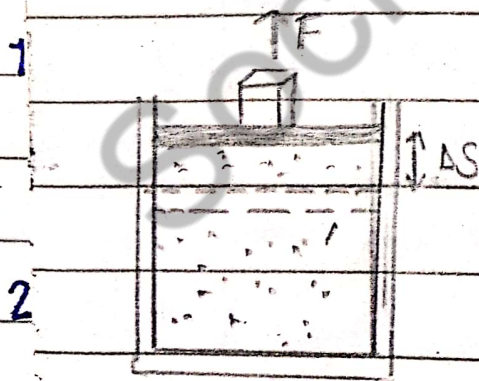
Work is defined as $\vec{F} \cdot \vec{\Delta S}$

TYPES OF THERMODYNAMIC WORK

WORK DONE BY THE SYSTEM

When system as a whole expands
system exert force on surround-
ing and displaces it

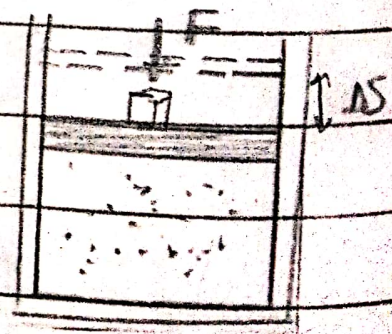
considered +ive



WORK DONE ON THE SYSTEM

When the system as a
whole contracts

considered as -ive



HEAT, WORK AND THERMAL ENERGY

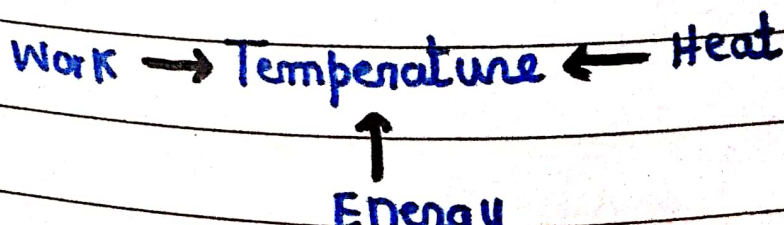
How heat, work and energy are closely related?

Each one of them is fundamentally related to temperature

Heat If the heat is given to a system, its temperature increases and if the heat is removed from the system, its temperature decreases

Work If we push the piston of the cylinder work is done on the system, it will hit the gas molecules, as a result K.E will increase which will increase the internal energy. This means, temperature will increase

Energy If heat energy is given to a system, the gas molecule will absorb the energy and increase their velocity, K.E will increase which will increase the internal energy and ultimately temperature will increase.



EQUIVALENCE OF HEAT

Count Rumford observed that heat could be produced in exhaustively by friction i.e. mechanical work. He showed that heat liberated was not related with mass but mechanical work.

In 1845 Joule carried an experiment to measure very precisely the quantity of heat produced by a certain amount of mechanical work. He showed that when a given amount of work is done, the same amount of heat always produced, no matter what may be the process of transformation.

given amount of work done \Rightarrow same amount of heat is produced

Work \propto Quantity of heat

$$W \propto Q$$

$$W = JQ$$

J = Mechanical Equivalent of heat = Joule's constant

Joule's Constant

“

The ratio of the work done in

joules to the heat produced in calories is called mechanical equivalent of heat”

$$J = \frac{W}{Q} = \frac{J}{\text{cal}}$$

When 'Q' is measured
in joule

$$J = \frac{W}{Q}$$

$$J = \frac{1 \text{ Joule}}{1 \text{ Joule}}$$

$$J = 1$$

When heat is measured
in calorie

$$J = \frac{W}{Q}$$

$$J = \frac{1 \text{ Joule}}{0.239 \text{ cal}}$$

$$J = 4.18 \text{ Joule/cal}$$

THERMODYNAMIC SYSTEM

→ A thermodynamic system is a system that includes any thing whose thermodynamic properties are of interest.

SYSTEM

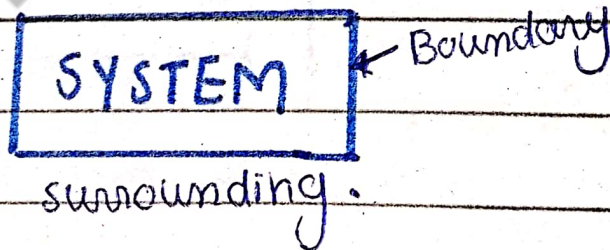
The quantity of matter or region of space whose behaviour is being studied

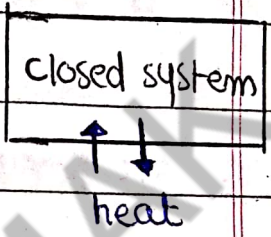
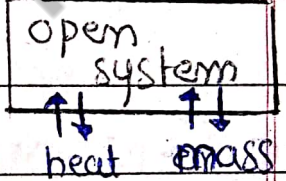
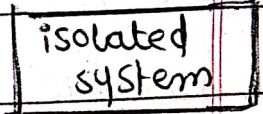
SURROUNDING

Everything other than system in the universe is called surrounding of the system.

BOUNDARY

A system is separated from surrounding by its boundary.



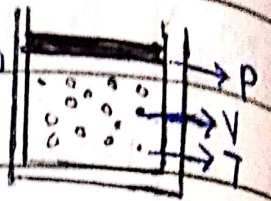
SYSTEM	MASS	HEAT	DIAGRAM
CLOSED SYSTEM	No transfer of mass across its boundary	Heat can be transferred from system to surrounding and vice versa	
OPEN SYSTEM	There is a transfer of mass across its boundary	transfer of energy can take place	
ISOLATED SYSTEM	No transfer of mass	No transfer of heat	

EXAMPLE

hot food in pressure cooker	boiling tea kettle	Tea contained in well insulating thermoblasts
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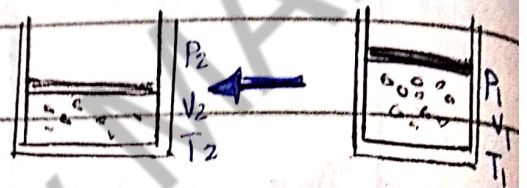
THERMODYNAMIC STATE

The particular condition when a system has specified value of pressure 'P', volume 'V' and temperature 'T' is called the state of the system.



STATE VARIABLE

The variables or functions which determine physical state of the system are called state variables.



HOMOGENEOUS SYSTEM

Temperature, pressure & volume are the state variables.

NON-HOMOGENEOUS SYSTEM

State variables are composition of system, temperature, pressure and volume.

EQUATION OF STATE SYSTEM

$$PV = nRT \Rightarrow \text{ideal gas equation}$$

The mathematical relationship b/w these state parameters is known as equation of state.

→ Exact relation b/w these parameters is not known for solids, liquids & non-homogeneous substances.

REVERSIBLE PROCESS

A process is said to be reversible if it can be **retracted** exactly in reverse order without producing any in the surrounding.

It is **slow** process.

There are **2 stages**, initial to final and final to initial.

It is in equilibrium in **all** stages.

Work obtained is **maximum**.

Energy loss is **less**.

IRREVERSIBLE PROCESS

A process which **cannot be retraced** in backward direction by reversing the controlling factors is said to be irreversible process.

It is **fast** process.

only **one stage** initial to final.

only initial and final stage is at equilibrium.

Work obtained is **minimum**.

Energy loss is **more**.

FOR REVERSIBLE PROCESS

Initial state $\xrightarrow[\text{Q}^+]{-W}$ Final state

- heat is added or absorbed $(+Q)$
- Work is done on the system $(-W)$

Final state $\xrightarrow[\text{Q}^-]{+W}$ Initial state

- heat is given out $(-Q)$
- Work is done by the system $(+W)$

THERMODYNAMIC PROCESS

change in state of system brought about by a change in state variables. The process occurs when a system interacts and exchanges energy within surroundings.

CYCLIC PROCESS

A series of processes which bring the system back to initial state is called cycle and the process is called cyclic process.

FIRST LAW OF THERMODYNAMICS ^{Est}

BASED ON: 1st law of thermodynamics is based on law of conservation of energy that energy can neither be created nor be destroyed.

⇒ It deals only with heat energy

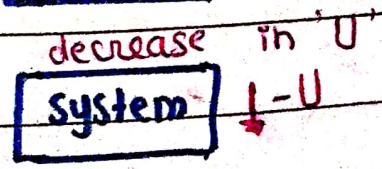
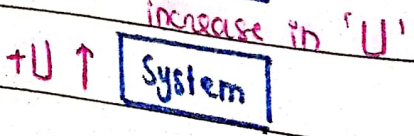
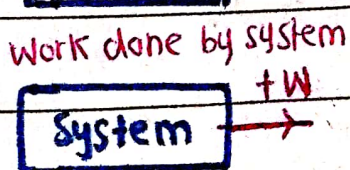
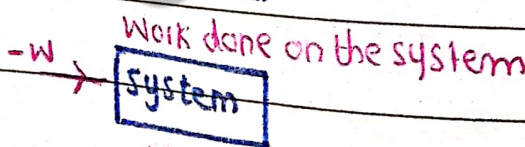
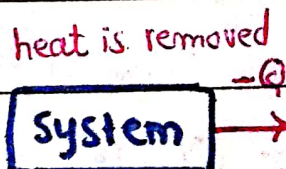
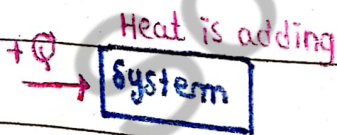
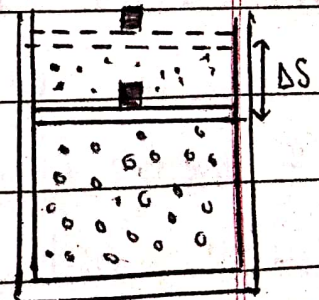
STATEMENT

“ In any thermodynamic process, when heat ' Q ' is added to a system, this energy appears as an increase in the internal energy ' ΔU ' stored in the system plus the work ' W ' done by the system on its surrounding ”

MATHEMATICALLY

$$\Delta Q = \Delta U + \Delta W$$

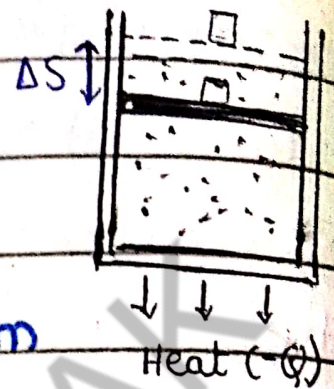
$$\Delta Q = (U_2 - U_1) + W$$



↑ ↑ ↑ ↑
Heat " Q "

When heat leaves the system

internal energy will decrease,
system will contract and work
is done on the system then



1st law of thermodynamics can
be written as:

$$-Q = -\Delta U - W$$

IMPORTANCE

1. The existence of an internal energy U as a state variable
2. The principle of conservation of energy
3. Heat as energy in transit

CHANGE IN INTERNAL ENERGY

change in internal energy of a system is equal to "energy flowing in as heat minus energy flowing out as work"

$$\Delta U = Q - W$$

81

• It is the energy **retained** by the system
When heat enters the system, a part of
it is consumed in doing work and the
remaining is internal energy $\Delta U = \Delta Q - \Delta W$

• Internal energy only depends upon the
initial and final state of system.

Internal Energy of cyclic process is zero

If a state $\Delta U = 0$

If a state of thermodynamics system is
changed from state to state then
change in internal energy of system is

$$\Delta U = U_B - U_A$$

U_A = initial internal energy

U_B = final internal energy

According to 1st law of

Thermodynamics

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta U = \Delta Q - \Delta W$$

$$[\because U_B - U_A = 0]$$

$$0 = \Delta Q - \Delta W$$

$$\Delta Q = \Delta W$$

→ All heat absorbed by system is used
in doing work by the system.

ISOCHORIC PROCESS | ISOBARIC PROCESS

DEFINITION

The thermodynamic process during which **volume** of system remains **constant**

The thermodynamic process during which **pressure** is kept **constant**

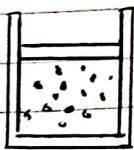
CONSTRUCTION

A cylinder having (1) ideal gas (2) conducting base (3) insulating walls (4) **Fixed insulating piston**

(4) **movable piston of cross-sectional area 'A'**

WORKING

1) heat is imparted to the gas ' ΔQ ' (2) internal energy of the system increases due to which temperature increases (3) Force is exerted on the walls of the cylinder so internal pressure increases (4) Initial states of the system are P_1, V_1, T_1 which will change into P_2, V_1, T_2 - volume remains constant (5) system neither contracts nor expands, so work is neither done by the system nor on the system $\Delta W = 0$



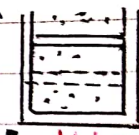
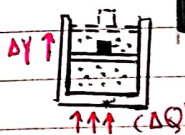
we consider 2 cases:

Isobaric expansion
work done by system

heat is given to the system, internal energy increases and exerts a force on the walls of cylinder, it will expand & piston moves upward. It covers some displacement Δy so work is done.

Isobaric compression

heat leaves the system ($-\Delta Q$) internal energy decreases, gas will compress & piston will move downward, volume is reduced and system contracts so work is done on the system.



MATHEMATICALLY

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta Q = \Delta U + 0 \Rightarrow \Delta Q = \Delta U$$

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta Q = \Delta U + P(\Delta V)$$

$\Delta V =$ increase in volume

$$W = F \cdot d$$

$$W = (PA)(\Delta y)$$

$$W = P(\Delta V)$$

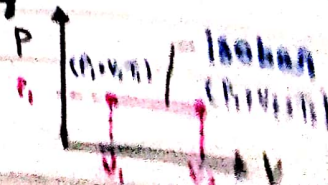
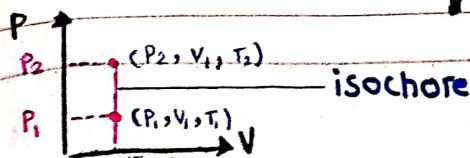
$$W = P \Delta V$$

CONCLUSION

- The entire amount of heat supplied to gas is converted to internal energy.
- on adding heat to system, internal energy, pressure & temperature increase.
- on removal of heat, internal energy decreases, system will cool down and pressure will fall.

- When gas expands, work is done by system, internal energy increases, temperature T_1 changes to T_2 and volume V_1 changes to V_2 .
- When gas contracts, work is done on system, internal energy, temperature and volume decrease.

P-V GRAPH



ISOTHERMAL PROCESS | ADIABATIC PROCESS

DEFINITION

The thermodynamic process in which **temperature** of system remains **constant**

The thermodynamic process during which **no heat** enters or leaves the system is called **adiabatic process**.

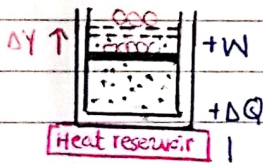
CONSTRUCTION

A cylinder having (1) ideal gas (2) conducting base (3) non-conducting walls (4) movable piston (5) heat reservoir at base of cylinder that maintains temp of gas at T_1

cylinder having (1) ideal gas (2) insulating wall, (3) insulating base (3) insulating movable piston

Isothermal Expansion

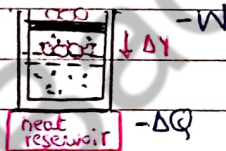
Let gas expand by decreasing pressure, internal energy of gas reduces which means its temperature is reduced so heat reservoir supply heat to gas so that temperature of system remains constant



Isothermal WORKING

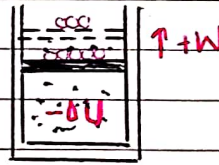
Compression

The gas is compressed by increasing the pressure, piston will move downward, internal energy increases so temp increases. Heat reservoir allow the heat to leave so that temperature is maintained.



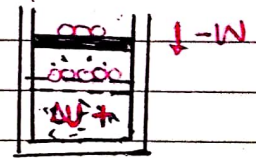
Adiabatic expansion

gas is expanded by decreasing pressure so work done by the system, temp will decrease, internal energy decreases and the gas will be cooled



Adiabatic compression

gas is compressed by increasing pressure so work is done on the system, temp will increase, internal energy increases, & gas will be heated



MATHEMATICALLY

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta U = 0$$

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta Q = 0$$

$$\Delta Q = 0 + \Delta W$$

$$V_1 < P_1$$

$$0 = \Delta U + \Delta W$$

$$\Delta Q = \Delta W$$

$$V_2 > P_2$$

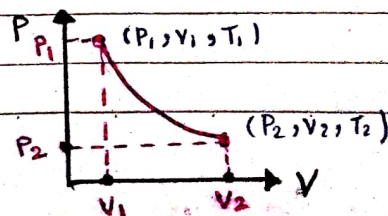
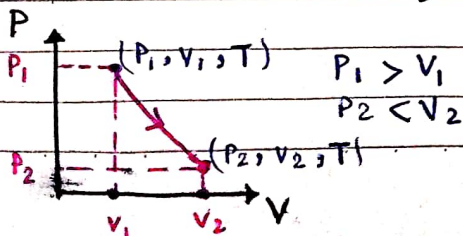
$$-\Delta U = \Delta W$$

CONCLUSION

- If gas expands, work is done by the system, heat has to be supplied to the gas
- If gas contracts, work is done on system, heat has to leave the gas

- If system does the work $+W$ internal energy decreases $-\Delta U = \Delta W$
- If work is done on the system, then internal energy increases $\Delta U = -\Delta W$

P-V GRAPH



PRACTICAL EXAMPLES

ISOCHORIC PROCESS

1. Fire crackers.
2. Pressure cooker
3. Otto cycle (gasoline air-mixture is burnt in car's engine)

ISOBARIC PROCESS

1. Boiling of water
2. Freezing of water

ISOTHERMAL PROCESS

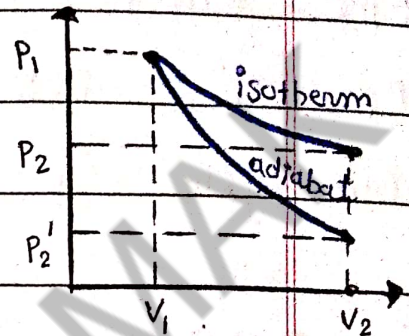
1. Refrigerator
2. heat pump

ADIABATIC PROCESS

1. cloud formation in atmosphere
2. Abrupt burst of tire

Why curve of adiabatic process is steeper than the curve in isothermal process?

Initially at volume V_1 the pressure of both are same but at final volume V_2 , the pressure of isothermal is high whereas that of adiabatic is very low. So



due to variation in pressure curve of adiabatic is steeper, (sharp variation in temp)

Isothermal Process

Initial states are P_1, V_1, T_1 . When gas was expanded, the pressure is decreased to P_2 and volume to V_2 while temp remains constant T_1 .

Adiabatic Process

Initial states are P_1, V_1, T_1 when gas expands at volume V_2 pressure decreases to P_2' , temp decreases to T_2 due to which internal energy decreases $T_2 < T_1$.

MATHEMATICAL PROOF

$$P_2 V_2 = nRT_1$$

$$P_2 = \frac{nR}{V_2} T_1$$

$$P_2' V_2 = nRT_2$$

$$P_2' = \frac{nR}{V_2} T_2$$

$$T_2 < T_1$$

$$P_2' < P_2$$

MOLAR SPECIFIC HEAT OF GAS

DEFINITION (Heat capacity)

The amount of heat energy required to raise the temperature of any substance through a unit degree is called heat capacity

MATHEMATICALLY

$$\Delta Q \propto \Delta T$$

$$\Delta Q = C \Delta T$$

$$\text{heat capacity} = \boxed{C = \frac{\Delta Q}{\Delta T}}$$

UNIT

$$J K^{-1}$$

SPECIFIC HEAT CAPACITY

The amount of heat required to raise the temperature of a unit mass of a substance through unit degree is called specific heat capacity

MATHEMATICALLY

$$\Delta Q \propto \Delta T \quad \text{--- (1)}$$

$$\Delta Q \propto m \quad \text{--- (2)}$$

combining eq (1) and (2)

$$\Delta Q \propto \Delta T m$$

$$\Delta Q = c \Delta T m$$

$$\boxed{c = \frac{\Delta Q}{\Delta T m}}$$

UNIT

$$J Kg^{-1} K^{-1}$$

MOLAR SPECIFIC HEAT CAPACITY

The quantity of heat required to raise the temperature of one mole of a gas by 1K is called molar specific heat.

MATHEMATICALLY

$$\Delta Q \propto \Delta T \quad \text{--- (1)}$$

$$\Delta Q \propto n \quad \text{--- (2)}$$

combining eq (1) and (2)

$$\Delta Q \propto \Delta T n$$

$$\Delta Q = C_m n \Delta T$$

$$C_m = \frac{\Delta Q}{n \Delta T}$$

C_m = molar specific heat capacity

UNIT = Joule mole⁻¹ K⁻¹

MOLAR SPECIFIC HEAT AT CONSTANT VOLUME

The amount of heat required to raise the temperature of one mole of gas by 1K while keeping its volume constant

$$\Delta Q_v = n C_v \Delta T$$

MOLAR SPECIFIC HEAT AT CONSTANT PRESSURE

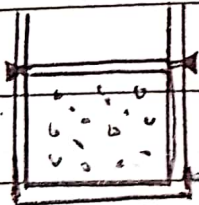
The amount of heat required to raise the temperature of one mole of gas by 1K while keeping its pressure constant

$$\Delta Q_p = n C_p \Delta T$$

Why $C_p > C_v$

AT CONSTANT VOLUME

When gas is heated at constant volume, its internal energy increases only but no work is done by the gas.



↑↑↑
Heat

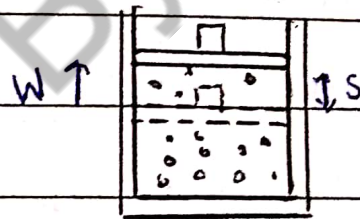
$$Q_v = \Delta Q_v$$

$$\Delta U = \Delta Q_v$$

$$\Delta U = C_v \Delta T$$

AT CONSTANT PRESSURE

When gas is heated at constant pressure, work is done with increase in internal energy. So more heat is required to get particular temperature.



↑↑↑
heat

$$Q_p = \Delta Q_v + W$$

$$\Delta U = \Delta Q_v$$

$$\Delta U = C_v \Delta T$$

AT CONSTANT VOLUME

If ΔQ_v is the amount of heat supplied and ΔT is the rise in temperature,

$$\Delta Q_v = n C_v \Delta T \quad \text{--- (1)}$$

According to 1st law of thermodynamics

$$\Delta Q_v = \Delta U + \Delta W_v$$

$$\Delta W_v = 0$$

$$\Delta Q_v = \Delta U + 0$$

$$\Delta Q_v = \Delta U \quad \text{--- (2)}$$

comparing eq (1) & (2)

$$\Delta U = n C_v \Delta T \quad \text{--- (3)}$$

AT CONSTANT PRESSURE

If ΔQ_p is the amount of heat supplied and ΔT is rise in temperature,

$$\Delta Q_p = n C_p \Delta T$$

According to 1st law of thermodynamics

$$\Delta Q_p = \Delta U + \Delta W_p$$

$$\Delta W_p = P \Delta V = n R \Delta T$$

$$\Delta Q_p = \Delta U + n R \Delta T$$

$$n C_p \Delta T = n C_v \Delta T + n R \Delta T$$

Dividing both sides by $n \Delta T$

$$\frac{n C_p \Delta T}{n \Delta T} = \frac{n C_v \Delta T}{n \Delta T} + \frac{n R \Delta T}{n \Delta T}$$

$$C_p = C_v + R$$

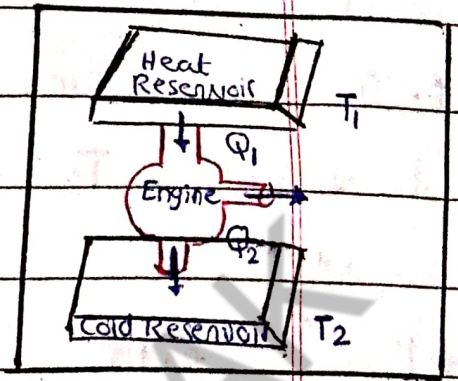
$$\boxed{C_p - C_v = R}$$

R = universal gas constant = $8.315 \text{ J mol}^{-1} \text{ K}^{-1}$

HEAT ENGINE

DEFINITION A device that converts heat energy into mechanical work

Heat Energy \rightarrow Mechanical Work



CONSTRUCTION

Heat Source or heat reservoir (HTR)

It is a source of heat energy and it is at high temperature T_1 . Its temperature remains constant during transfer of heat in or out.

Heat Sink or cold reservoir (LTR)

It is a body at low temperature T_2 . Its temperature remains constant.

Working Substance

Gas is used as working substance which is taken through cyclic process.

WORKING

1. Heat engine work b/w hot and cold body
2. Engine gains heat energy Q from HTR at temperature T_1

3. It converts part of heat energy into mechanical work

4. The remaining part Q_2 is rejected to LTR at temperature T_2

→ Heat engine is made to operate in cyclic process to get continuous steady mechanical energy

MATHEMATICALLY

In cyclic process

$$\Delta U = 0$$

According to 1st law of thermodynamics

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta Q = 0 + \Delta W$$

$$\Delta Q = \Delta W$$

$$Q_1 - Q_2 = \Delta W$$

Q_1 = heat energy absorbed by heat engine to HT

Q_2 = heat energy rejected by heat engine to LTR

EFFICIENCY OF HEAT ENGINE

The ratio of net work done to the heat absorbed by the engine

MATHEMATICALLY

$$\text{Efficiency} = \frac{\text{Work done by the engine}}{\text{Heat absorbed by the engine}}$$

$$\eta = \frac{\Delta W}{Q_1}$$

$$\eta = \frac{Q_1 - Q_2}{Q_1}$$

$$\eta = \frac{Q_1}{Q_1} - \frac{Q_2}{Q_1}$$

$$\eta = 1 - \frac{Q_2}{Q_1}$$

IDEAL CASE

If no heat exhausted by engine so that all the heat Q_1 absorbed were converted to work ($Q_2 = 0$)

$$\eta = 1 - \frac{0}{Q_1}$$

$$\eta = 1 - 0$$

$$\eta = 1$$

$$\eta = 1 \times 100$$

$$\eta = 100\%$$

2nd LAW OF THERMODYNAMICS

- * 2nd law of thermodynamics gives the verification of 1st law of thermodynamics.
- * specifies direction to flow of heat.
- * gives method for conversion of heat into work.
- * Based on natural law.

LORD KELVIN STATEMENT

“It is impossible to construct a heat engine, operating continuously in a cycle which takes heat from heat source at higher temperature and performs an equivalent amount of work without rejecting any heat to heat sink at low temperature.”

RUDOLF CLAUSIUS STATEMENT

“It is impossible to cause heat to flow from a cold body to hot body without the expenditure of work.”

Work performed < heat absorbed

CARNOT HEAT ENGINE

In 1824 Sadi Carnot introduced a theoretical engine to improve efficiency of heat engine.

CONSTRUCTION

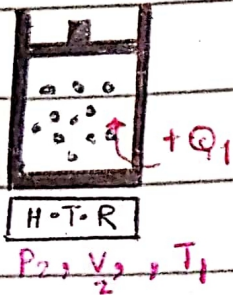
1. cylinder that contains gas with movable piston
2. Insulated piston and walls
3. conducting base.

CARNOT CYCLE

Carnot engine operates in a cycle known as Carnot cycle. It consists of 4 steps:

1. Isothermal Expansion
2. Adiabatic Expansion
3. Isothermal Compression
4. Adiabatic compression

ISOTHERMAL EXPANSION



1. The working system is at pressure P_1 volume V_1 , temperature T_1

2. The gas is placed on H.T.R. at T_1 absorbing heat $+Q$ keeping temperature constant

3. By expanding the gas, pressure decreases from P_1 to P_2

4. Volume increases from V_1 to V_2

5. Temperature remain T_1

ADIABATIC EXPANSION



1. The working system is at pressure P_2 volume, temperature T_2

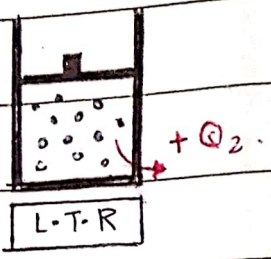
2. The gas cylinder is placed on an insulating stand. No heat enters or leaves the system

3. By expanding gas, pressure decreases from P_2 to P_3

4. Volume increases from V_2 to V_3

5. In this case work is done by the system so internal energy decrease and temp falls from T_2

ISOTHERMAL COMPRESSION



P_3, V_3, T_2

The working system is at pressure P_3 , volume V_3 temp T_2

The gas cylinder is placed at T_2 , rejecting heat $-Q$ keeping temp constant

the gas compress, pressure increases from P_3 to P_4

Volume reduces from V_3 to V_4

temperature remain T_2

ADIABATIC COMPRESSION



P_4, V_4, T_1

1. The working system is at pressure P_4 volume V_4 temp T_1

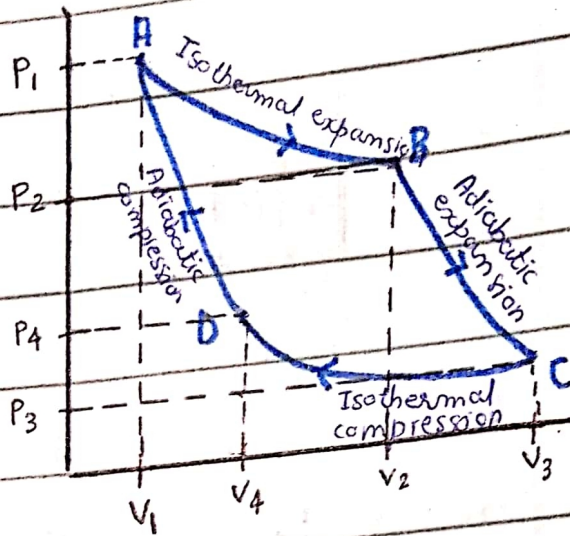
2. The gas cylinder is placed at insulating stand so no heat can enter or leave system

3. Let the gas compress, pressure increases from P_4 to P_1 (return to its initial state)

4. Volume reduces from V_4 to V_1

5. work is done on the system so internal energy increases due to which temp increases from T_2 to T_1

GRAPHICAL REPRESENTATION



EFFICIENCY

Q_1 = heat absorbed during isothermal expansion
 Q_2 = heat rejected during isothermal compression

$$\Delta W = Q_1 - Q_2$$

Area ABCD = represent the work done by engine in one cycle.

$$\eta = \frac{\text{work obtained}}{\text{heat supplied}}$$

$$\eta = \frac{\Delta W}{Q_1}$$

$$\eta = \frac{Q_1 - Q_2}{Q_1}$$

$$\eta = \frac{Q_1}{Q_1} - \frac{Q_2}{Q_1}$$

$$\eta = 1 - \frac{Q_2}{Q_1}$$

$$\therefore \frac{Q_2}{Q_1} = \frac{T_2}{T_1}$$

$$\eta = 1 - \frac{T_2}{T_1}$$

• If ratio is small then efficiency will be greater

• If ratio is bigger then efficiency will be less

CARNOT THEOREM

STATEMENT-1

No heat engine is more efficient than Carnot engine working b/w 2 same temperature.

STATEMENT-2

All Carnot and reversible engine have same efficiency when they are working b/w 2 same temperature.

REFRIGERATOR

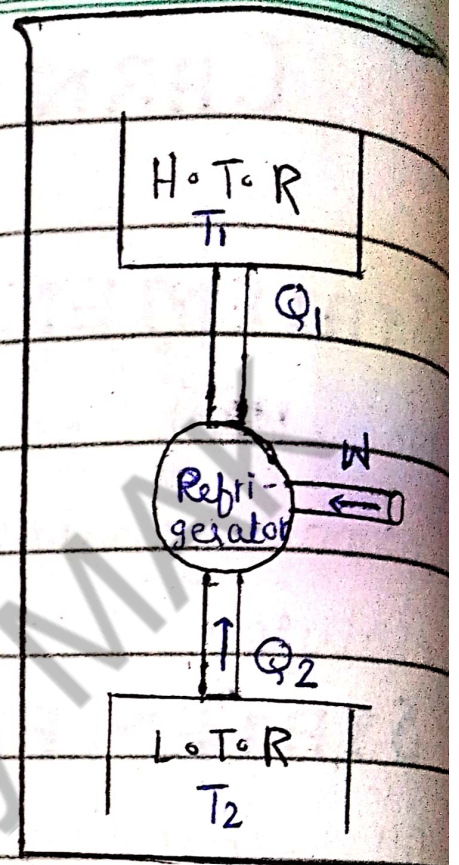
“The device which will either cool or maintain a body temperature below that of surrounding is called refrigerating machine.”

1. The working substance performs cycle in a direction opposite to that of a heat engine.
2. It takes heat from L.T.R and ejects it to H.T.R with expenditure of work.

WORKING

1. The amount of heat Q_2 is removed from L.T.R at temperature T_2

2. A work W is performed by the compressor of the refrigerator on the refrigerant



3. The quantity of heat Q_1 is rejected to H.T.R at temperature T_1

$$Q_1 = W + Q_2$$

4.

$$Q_1 - Q_2 = W$$

CO-EFFICIENT OF PERFORMANCE

The ratio of amount of heat removed from the heat sink to the work required to do so.

COOLING ENERGY RATIO

$$\eta_{\text{cooling}} = \frac{Q_2}{W}$$

$$\beta_{\text{cooling}} = \frac{Q_2}{Q_1 - Q_2}$$

$$\eta_{\text{cooling}} = \frac{T_2}{T_1 - T_2}$$

HEATING ENERGY RATIO

$$\eta_{\text{heating}} = \frac{Q_1}{W}$$

$$\eta_{\text{heating}} = \frac{Q_1}{Q_2 - Q_1}$$

$$\eta_{\text{heating}} = \frac{T_1}{T_2 - T_1}$$

ENTROPY

DEFINITION

“The measure of randomness or disorderliness of the system is called entropy.”

Randomness \propto Entropy

EXAMPLE

consider a container having gas molecules. When heat is given, the random motion of molecules will increase, disorderliness will increase which mean entropy will increase.

MATHEMATICALLY

$$\Delta S = \frac{\Delta Q}{T} = \frac{J}{K} = JK^{-1}$$

ΔQ = Amount of heat which system absorb or reject.

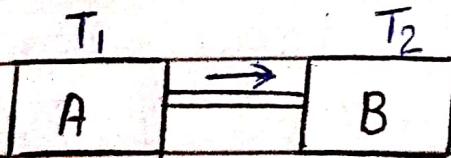
SIGN CONVENTION

- If heat is added = $+\Delta Q$ = Entropy ($+\Delta S$) increases
- If heat is rejected = $-\Delta Q$ = Entropy ($-\Delta S$) decreases

STATE FUNCTION

- Entropy is state function, independent of path followed
- depends only on initial and final state of system $\Delta S = S_f - S_i$

EXAMPLE



consider 2 systems A and B having temperatures T_1 and T_2 respectively. which are connected through conducting rod. Heat flows from system A at

temperature T_1 to system B at Temperature T_2 . $T_1 > T_2$ so system A loses the heat and system B gains the heat .

$$S_1 = \frac{Q_1}{T_1}$$

$$S_2 = \frac{Q}{T_2}$$

$$\Delta S = S_2 - S_1$$

$$\Delta S = \frac{Q}{T_2} - \frac{Q}{T_1} \quad \frac{Q}{T_2} > \frac{Q}{T_1}$$

$\Delta S =$ positive (entropy increases)

natural process , the entropy will always increase of the universe

$$\Delta S_{universe} = \Delta S_{system} + \Delta S_{surrounding}$$

4th LAW OF THERMODYNAMICS IN TERMS OF ENTROPY

If a system undergoes a natural process, it will go in the direction that causes the entropy of system plus the environment to increase ."

REVERSIBLE PROCESS

Entropy = constant

$$\Delta S = 0$$

IRREVERSIBLE PROCESS

Entropy increases

DEGRADATION OF ENERGY

In all natural processes, energy tends to pass from a more useful form to a less useful form. This is called "degradation of energy."

ADIABATIC EQUATION

According to 1st law of thermodynamics

$$\Delta Q = \Delta U + \Delta W$$

$$0 = \Delta U + \Delta W$$

$$0 = \Delta U + P \Delta V$$

$$0 = n C_V \Delta T + P \Delta V$$

$$n C_V (\Delta T) = -P \Delta V$$

$$n C_V \left[\frac{\Delta P V}{n R} \right] = -P \Delta V$$

$$W = F \cdot d$$

$$W = (P A) \Delta Y$$

$$W = P \Delta V$$

$$P V = n R T$$

$$\Delta P V = n R \Delta T$$

$$\frac{\Delta P V}{n R} = \Delta T$$

$$C_V \frac{\Delta P V}{R} = -P \Delta V$$

$$C_V \frac{\Delta P}{P} = -\frac{\Delta V}{V} R$$

$$C_V \frac{\Delta P}{P} = -\frac{\Delta V}{V} (C_P - C_V) \quad (\because C_P - C_V = R)$$

$$\frac{\Delta P}{P} = -\frac{\Delta V}{V} \left(\frac{C_P - C_V}{C_V} \right)$$

$$\frac{\Delta P}{P} = -\frac{\Delta V}{V} \left(\frac{C_P}{C_V} - \frac{C_V}{C_V} \right)$$

$$\frac{\Delta P}{P} = -\frac{\Delta V}{V} (\gamma - 1) \quad (\because \frac{C_P}{C_V} = \gamma)$$

$$\frac{\Delta P}{P} = -\frac{\Delta V}{V} \gamma + \frac{\Delta V}{V} \rightarrow 0 \quad \left[\frac{\Delta V}{V} \approx 0 \right]$$

$$\frac{\Delta P}{P} = -\frac{\Delta V}{V} \gamma$$

Applying integration

$$\int \frac{\Delta P}{P} = -\gamma \int \frac{\Delta V}{V}$$

$$\ln P = -\gamma \ln V + \ln C$$

$$\ln P = -\ln V^\gamma + \ln C$$

$$\ln P + \ln V^\gamma = \ln C$$

$$\ln PV^\gamma = \ln C$$

$$(\because \log A + \log B = \log A \times B)$$

$$\Rightarrow PV^\gamma = C$$

$$PV^\gamma = \text{constant}$$